

## C7L1 Notes

### The Inverse Sine, Cosine, and Tangent Functions

$$\begin{array}{llll} y = \arcsin x & \text{IFF} & \sin y = x & \text{D: } -1 \leq x \leq 1 & \text{R: } \frac{-\pi}{2} \leq y \leq \frac{\pi}{2} \\ y = \arccos x & \text{IFF} & \cos y = x & \text{D: } -1 \leq x \leq 1 & \text{R: } 0 \leq y \leq \pi \\ y = \arctan x & \text{IFF} & \tan y = x & \text{D: } -\infty < x < \infty & \text{R: } \frac{-\pi}{2} < y < \frac{\pi}{2} \end{array}$$

### Properties of Inverse Functions

If  $-1 \leq x \leq 1$

then  $\sin(\arcsin x) = x$

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If  $\frac{-\pi}{2} \leq y \leq \frac{\pi}{2}$

then  $\arcsin(\sin y) = y$

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If  $-1 \leq x \leq 1$

then  $\cos(\arccos x) = x$

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If  $0 \leq y \leq \pi$

then  $\arccos(\cos y) = y$

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If  $-\infty < x < \infty$

then  $\tan(\arctan x) = x$

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If  $\frac{-\pi}{2} < y < \frac{\pi}{2}$

then  $\arctan(\tan y) = y$

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$\arcsin x = \sin^{-1}x$	$\arccos x = \cos^{-1}x$	$\arctan x = \tan^{-1}x$
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